

---

# **CSC 580**

# **Cryptography and Computer Security**

*Authenticated Encryption, Key Wrapping, and PRNGs  
(Sections 12.6-12.9)*

---

April 3, 2018

---

# Goal: Protect both Confidentiality and Integrity

---

Some techniques that have been used:

- Encrypt with hash of message:  $E(K, M \parallel H(M))$ 
  - *E better be non-malleable!! (problem with WEP using RC4)*
- Encrypt with MAC:  $E(K_1, M \parallel \text{MAC}(K_2, M))$ 
  - *Used in SSL/TLS*
- Encrypt followed by MAC:  $C = E(K_1, M) ; T = \text{MAC}(K_2, C)$ 
  - *Used in IPSec*
- Encrypt and MAC:  $C = E(K_1, M) ; T = \text{MAC}(K_2, M)$ 
  - *Used in SSH*

Notes:

- Important to use different keys for encryption and MAC (avoid interactions)
  - All techniques have drawbacks
-

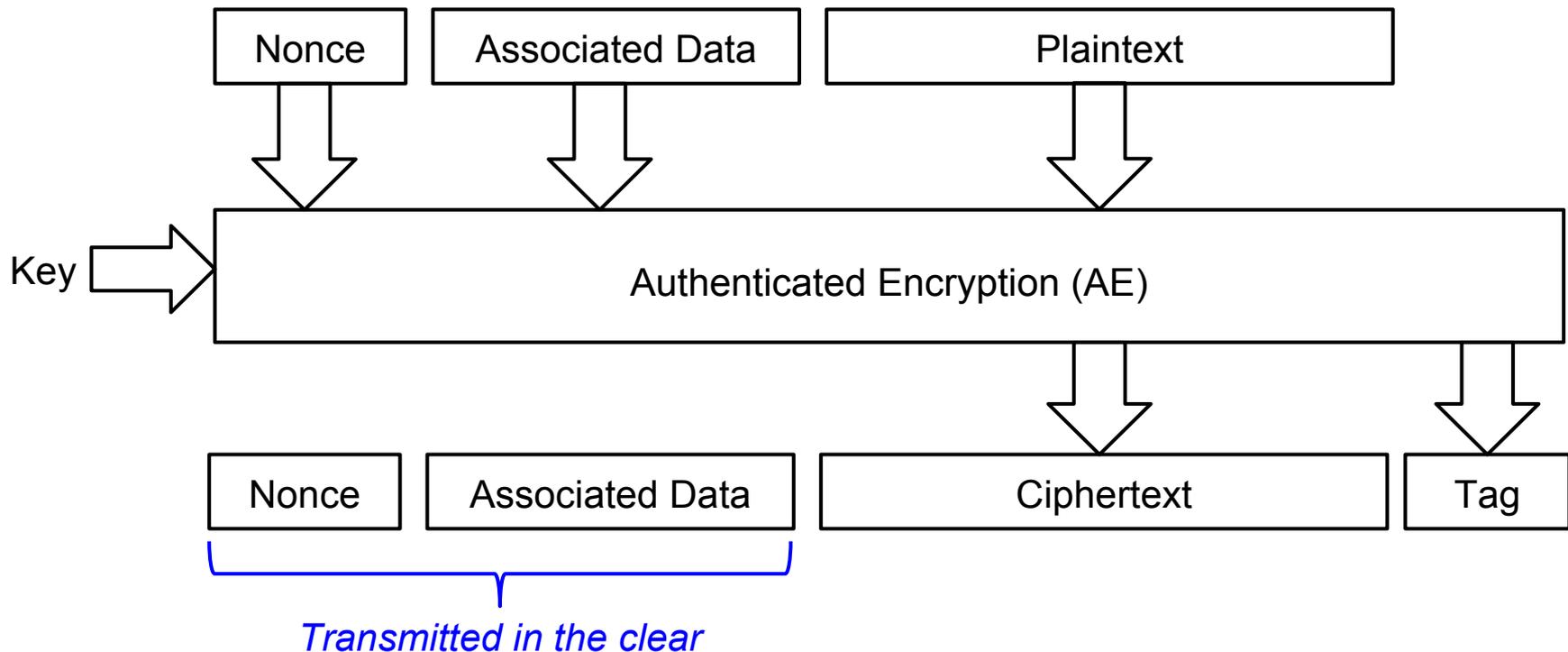
# New and Improved! Authenticated Encryption

## High-Level Idea

---

### Ideas:

- Design for confidentiality and integrity together - use a single key!
- Allow some data to be transmitted in the clear, but still authenticated



# JCA - Using Authenticated Encryption

## Example using GCM (one AE mode)

---

```
GCMParameterSpec s = ...;
cipher.init(..., s);

// If the GCM parameters were generated by the provider, it can
// be retrieved by:
// cipher.getParameters().getParameterSpec(GCMParameterSpec.class);

cipher.updateAAD(...); // AAD (optional - must be before plaintext)
cipher.update(...);    // Multi-part update
cipher.doFinal(...);   // conclusion of operation

// Use a different IV value for every encryption
byte[] newIv = ...;
s = new GCMParameterSpec(s.getTLen(), newIv);
cipher.init(..., s);
...
```

On encryption: Tag is embedded in output ciphertext (you don't have to handle!)

On decryption: Bad tag results in throwing `AEADBadTagException`

---

# Two AE modes: CCM and GCM

---

## CCM (Counter with CBC-MAC)

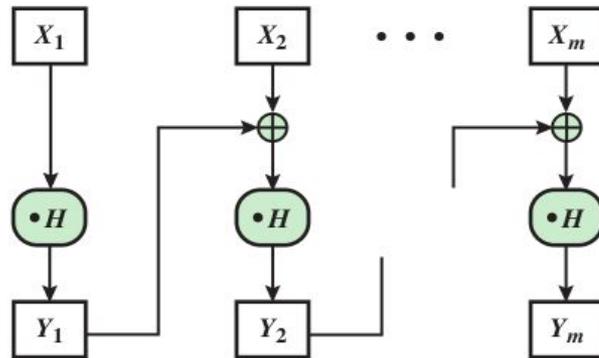
- Ciphertext produced using CTR mode
- MAC produced using CBC-based MAC
- The good: Strong, provable security under certain assumptions
- The bad:
  - Encrypt/MAC require two independent block cipher calls
  - Inclusion of CBC means not parallelizable

## GCM (Galois/Counter Mode)

- CTR mode encryption - *almost...* incr 32-bits →  $2^{39}$ -bit limit on size
  - GHASH to auth ciphertext - one Galois Field (GF) mult per block
  - The good:
    - Strong, provable security under certain assumptions
    - Per block: 1 block cipher call, and one GF mult (Intel instruction) - fast!
    - Block cipher calls are parallelizable (just like CTR mode)
  - The bad: ?
-

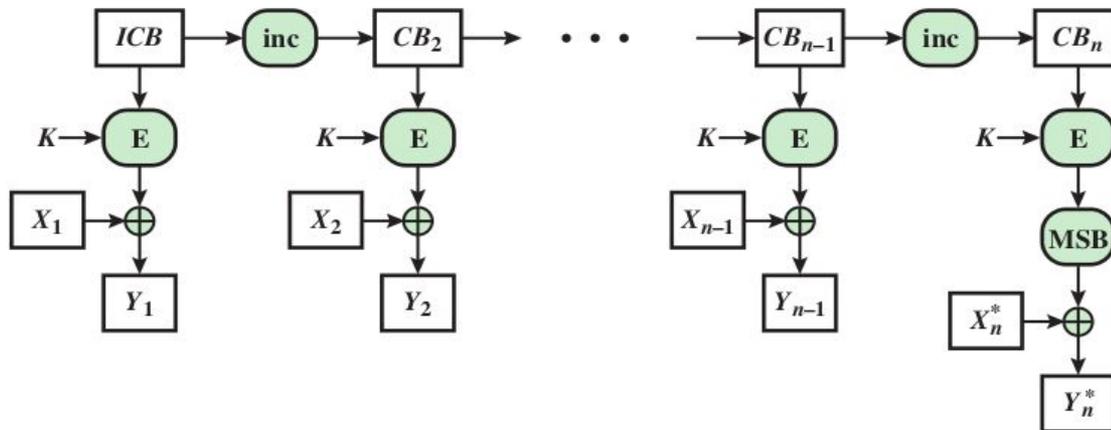
# GCM - Algorithm Overview

## Hash and Encryption Functions



A little misleading: When combined, these  $X_i$ 's are *ciphertext* blocks (called  $Y_i$  below)!

(a)  $\text{GHASH}_H(X_1 \parallel X_2 \parallel \dots \parallel X_m) = Y_m$



(b)  $\text{GCTR}_K(\text{ICB}, X_1 \parallel X_2 \parallel \dots \parallel X_n^*) = Y_1 \parallel Y_2 \parallel \dots \parallel Y_n^*$

Figure 12.10 GCM Authentication and Encryption Functions

# GCM - Algorithm Overview

## Overall GCM operation

---

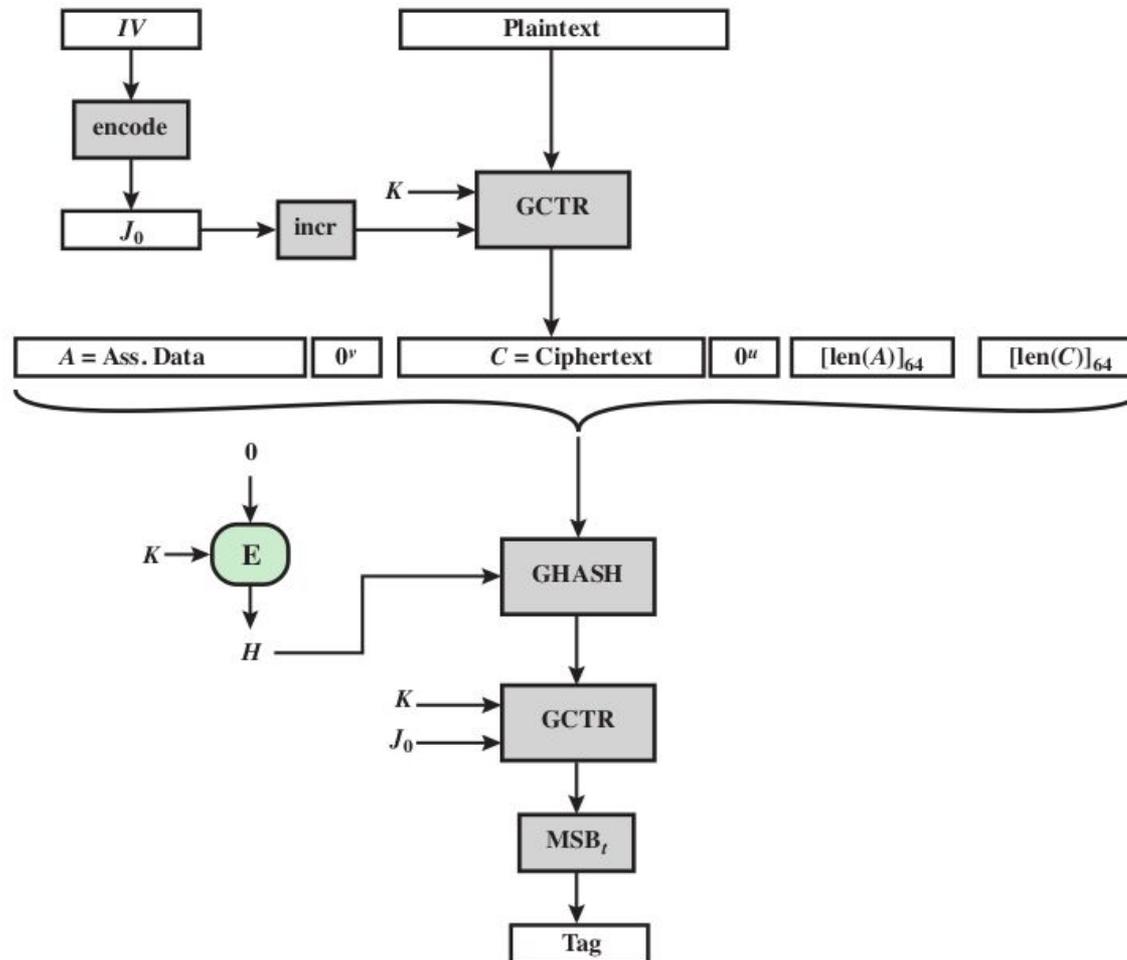


Figure 12.11 Galois Counter - Message Authentication Code (GCM)

# Key Wrapping

---

Consider: In the JCA KeyStore, keys are stored in a file. How are they protected?

- Password used to “unlock” the KeyStore
- Need to use encryption with one key to encrypt another key
- An AES 256-bit key spans multiple blocks of AES
- Can a specially designed mode help?
  - Advantage: Limited size plaintext (can have all in memory at once)
  - Speed isn't as big an issue as it is with bulk encryption
  - Wrapped key is random - how do you know decryption is right - authentication!
  - Specially designed mode: Key Wrap (KW) mode

Related notions with different terminology:

- **Key Wrapping**: Encrypting a symmetric key using symmetric cipher
  - **Key Encapsulation**: Encrypting a symmetric key using a public key algorithm (e.g., for hybrid encryption)
-

# AES Key Wrap Mode

## Pseudocode from NIST publication

---

**Inputs:** Plaintext,  $n$  64-bit values  $\{P_1, P_2, \dots, P_n\}$ ,  
Key,  $K$  (the KEK).

**Outputs:** Ciphertext,  $(n+1)$  64-bit values  $\{C_0, C_1, \dots, C_n\}$ .

1) Initialize variables

Set  $A^0 = IV$ , an initial value (see 2.2.3)

For  $i = 1, \dots, n$

$$R_i^0 = P_i$$

2) Calculate intermediate values

For  $t = 1, \dots, s$ , where  $s = 6n$

$$A^t = \text{MSB}_{64}(\text{AES}_K(A^{t-1} | R_1^{t-1})) \oplus t$$

For  $i = 1, \dots, n-1$

$$R_i^t = R_{i+1}^{t-1}$$

$$R_n^t = \text{LSB}_{64}(\text{AES}_K(A^{t-1} | R_1^{t-1}))$$

3) Output the results

Set  $C_0 = A^t$

For  $i = 1, \dots, n$

$$C_i = R_i^t$$

Default IV is hex:

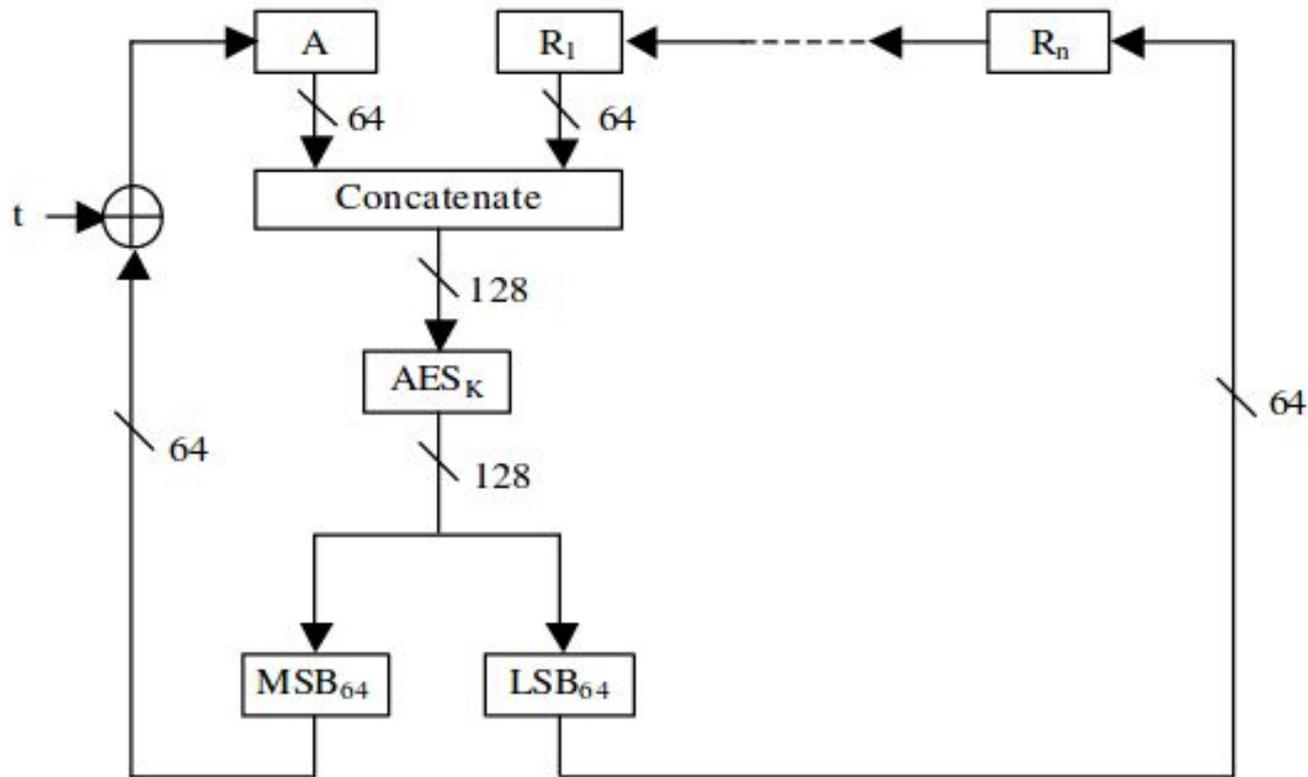
A6

Each 64-bit plaintext block gets “shifted through” encryption position 6 times.

# AES Key Wrap Mode

Diagram of one stage (from NIST)

---



# PRNGs from Hash Functions and MACs

---

## Observations:

- PRNGs need uniformly distributed output
  - Good hash functions and MACs have uniformly distributed outputs
- PRNGs need to be one-way so seed/state can't be derived
  - Good hash functions and MACs are preimage resistant (one-way)
- PRNGs need output to be computationally uncorrelated (independent)
  - Good hash functions and MACs have collision resistance

And in addition: Hash functions and MACs tend to be fast

So.... Can we use hash functions and MACs to make good PRNGs?

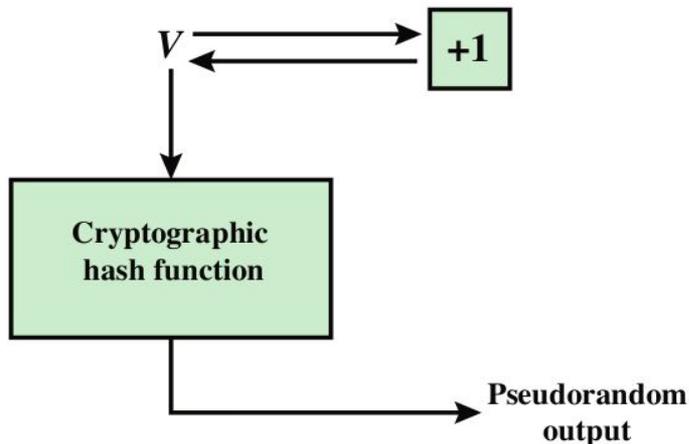
---

# PRNGs from hash functions

---

Idea: Concatenate seed and counter, and run through hash fn

So: Initialize  $V = \text{seed} \parallel 0$



(a) PRNG using cryptographic hash function

*From Figure 12.14 in the textbook*

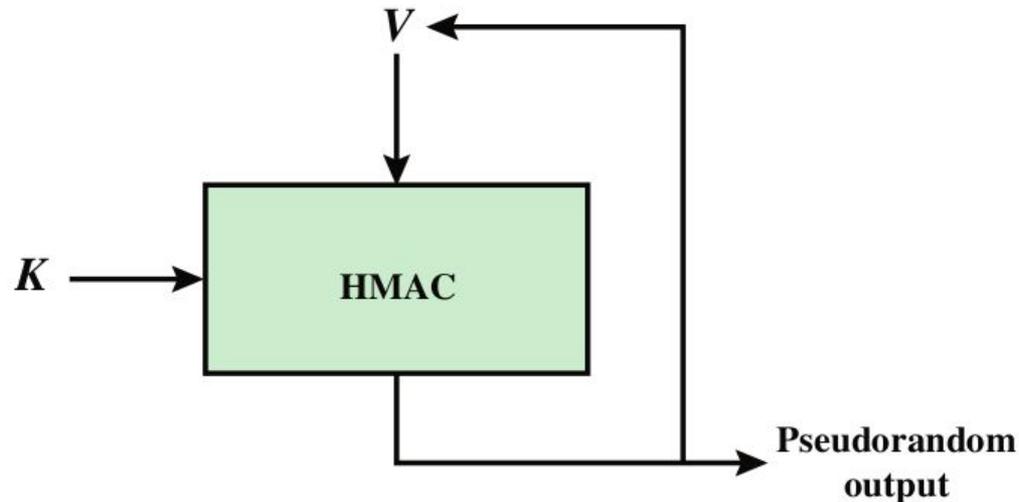
This is essentially how the standard Java SHA1PRNG instance of SecureRandom works (generally the default)

---

# PRNGs from MACs

---

Can use a simple feedback loop with a MAC (NIST SP 800-90)



(b) PRNG using HMAC

Some other options

- Can use a MAC with a counter, like previous slide (IEEE 802.11i does this)
  - Can do feedback, but concatenate a constant (the seed) each iteration (TLS)
-